Automatic Knowledge Transfer for Agent-based Bilateral Negotiation Tasks

Shuang Zhou, Siqi Chen, Evgueni Smirnov, Gerhard Weiss
Maastricht University
P.O. Box 616, 6200 MD Maastricht, The Netherlands
{shuang.zhou, siqi.chen, smirnov, gerhard.weiss}@maastrichtuniversity.nl

Karl Tuyls
University of Liverpool
Ashton Street, Liverpool L69 3BX, United Kingdom
k.tuyls@liverpool.ac.uk

ABSTRACT

Learning opponents is an important problem in multi-issue automated negotiation. However it is a difficult problem due to (1) the indirect way the target function can be observed, and (2) the limited amount of experience available to learn from an unknown opponent at a single session. To address these difficulties we propose to adapt two approaches from transfer learning. Both approaches transfer knowledge from previous sessions to current negotiation session of an agent when learning the latent behaviour model of the opposing agent. The first approach transfers by weighting the encounter offers of previous and ongoing sessions while the second one by weighting the models learnt from the previous negotiation sessions and the model learnt from the current negotiation session. Experimental results show the applicability and effectiveness of both approaches. Moreover, the robustness of the proposed approaches is evaluated using empirical game theoretic analysis.

Keywords
Automated Multi-issue Negotiation; Transfer Learning; Sparse Pseudo-input Gaussian Processes; Empirical Game Theoretic Analysis

1. INTRODUCTION

In automated negotiation two or more agents try to come to a joint agreement in a consumer-provider or buyer-seller set-up [13]. One of the biggest driving forces behind research into automated negotiation is the broad spectrum of potential applications. Various negotiation settings differentiate themselves through, for instance, the number of participants (i.e. bilateral or multilateral), or the number of issues being negotiated upon (i.e. whether a single or multiple issues are the subject of each placed bid). While the contributions from this work are (at least in principle) applicable to multilateral negotiations, the paper focusses on bilateral, multi-issue negotiation mainly because this makes the proposed techniques easier to explain. The interaction framework enforced in automated negotiations (see Section 2.1) lends itself to the use of machine learning techniques for opponent modelling. The driving force of an (opposing) agent is governed by its hidden utility function through its also hidden bidding strategy. Given the behaviour model of an opposing agent, an agent can reach better final (or cumulative) agreement terms by exploiting this knowledge. However, learning an opposing agent’s behaviour model is not a trivial work since

1Because both an agent’s utility function and bidding strategy are hidden, we will often use the term behaviour model to encompass both as the force governing the agents negotiating behaviour.

1. the behaviour model can only be observed indirectly through offers refused and counter offers made by the opposing agent
2. the amount of encounter offers available to learn from in a single negotiation session is limited.

To address these two problems simultaneously we make use of transfer learning techniques. Transfer learning is a branch of machine learning that enables the use of knowledge learned in a previous task (so called source task) to aid learning in a different, related new task (target task) [17]. One of the main goals of transfer learning is to reach better performance by transferring knowledge from source task when few target data available, which makes it ideally suited for learning settings like that of automated negotiation. The learning of an opponent model in the ongoing negotiation (target task) can be benefit from transferring knowledge from previous negotiations (source tasks). Aiming at applying transfer learning to automated negotiation, this work contributes by:

1. proposing a generic strategy framework for agent-based negotiation;
2. modifying an instance-based transfer algorithm TrAdaBoost [8] for multi-issue negotiation problems, and

Experiments performed on various challenging negotiation tasks show that transfer can aid target agents in improving their behaviours once encountering new opponents varying in their preference profiles, bidding strategies, and/or utility functions. The contributions also includes the discussion of performance improvement resulting from transfer, which opens up a few new directions of research.

The remainder of this paper is structured as follows. Section 2 underlines the background of our research. Section 3 proposes the generic strategy framework for automated negotiation and the two transfer learning schemes. Section 4 offers extensive experimental results and a game-theoretical analysis of the proposed learning approaches. Section 5 provides related work. Section 6 identifies some important research lines outlined by our paper and concludes the work.

2. PRELIMINARIES

This section provides necessary background knowledge for the remainder of this paper. In order, it sketches the framework of bilateral negotiations, presents the needed preliminaries and notations
for Sparse Pseudo-input Gaussian Processes as a regression technique, and introduces the instance-based and model-based transfer learning approaches.

2.1 Bilateral Negotiation

The automated negotiation framework adopted in this work is a basic bilateral multi-issue negotiation model as it is widely used in the agents field (e.g., [6, 7, 24]). The negotiation protocol is based on a variant of the alternating offers protocol proposed in [21], where the negotiation process is limited by a certain number of rounds.

Let \( I = \{a, b\} \) be a pair of negotiating agents, where \( i \) (\( i \in I \)) is used to represent any of the two agents. The goal of \( a \) and \( b \) is to establish a contract for a product or service, where a contract consists of a vector of issue values. Inherent to the negotiation process is that agents \( a \) and \( b \) act in conflictive roles. To make this precise, let \( J \) be the set of issues under negotiation where \( j \) (\( j \in \{1, ..., n\} \)) is used to represent a particular issue. Contracts are tuples \( O = (O_1, ..., O_n) \) that assign a value \( O_j \) to each issue \( j \). A contract is said to be established if both agents agree on it. Following Rubinstein’s alternating bargaining model, each agent makes, in turn, an offer in form of a contract proposal.

Each agent \( i \) decides to accept or reject an offer based on a weight vector \( w^i = (w^i_1, ..., w^i_n) \) (also called importance vector or preference vector) that represents the relative importance of each issue \( j \in \{1, ..., n\} \). These weights are usually normalized (i.e., \( \sum_{j=1}^{n} w^i_j = 1 \) for each agent \( i \)).

The utility of an offer for agent \( i \) is obtained by the utility function, defined as:

\[
U^i(O) = \sum_{j=1}^{n} (w^i_j \cdot V_j^i(O_j))
\]  

where \( w^i_j \) and \( O \) are as defined above and \( V_j^i \) is the evaluation function for \( i \), mapping every possible value of issue \( j \) (i.e., \( O_j \)) to a real number. The two parties continue exchanging offers till an agreement is reached or negotiation time runs out.

2.2 Sparse Pseudo-input Gaussian Processes

Gaussian Processes (GPs) are a form of non-parametric regression techniques. Following the notation of [19], given a data set \( D = \{x^{(i)}, y^{(i)}\}_{i=1}^{m} \) where \( x \in \mathbb{R}^d \) is the input vector, \( y \in \mathbb{R} \) the output vector and \( m \) is the number of available data points when a function is sampled according to a GP, we write, \( f(x) \sim \mathcal{GP}(m(x), k(x, x')) \), where \( m(x) \) is the mean function and \( k(x, x') \) the covariance function, together fully specifying the GP. Learning in a GP setting involves maximizing the marginal likelihood of Equation 2.

\[
\log p(y|X) = \frac{1}{2} y^T \left( K + \sigma_n^2 I \right)^{-1} y - \frac{1}{2} \log |K + \sigma_n^2 I| - \frac{n}{2} \log 2\pi,
\]

where \( y \in \mathbb{R}^{m \times 1} \) is the vector of all collected outputs, \( X \in \mathbb{R}^{m \times d} \) is the matrix of the data set inputs, and \( K \in \mathbb{R}^{m \times m} \) is the covariance matrix with \( |\cdot| \) representing the determinant. The interested reader should refer to [19] for a more thorough discussion of the topic. To fit the hyperparameters that best suit the available data set we need to maximize the marginal likelihood function of Equation 2 with respect to \( \Theta \) the vector of all hyperparameters. Typically, this maximization requires the computation of the derivatives of Equation 2 with respect to \( \Theta \). These derivatives are then used in a gradient-based algorithm to perform the updates to the hyperparameters \( \theta_j \) using the following set of equations:

\[
\frac{\partial}{\partial \theta_j} \log p(y|X, \Theta) = \frac{1}{2} y^T K^{-1} \partial K \partial \theta_j y - \frac{1}{2} \text{tr} \left( K^{-1} \partial K \partial \theta_j \right)
\]  

\[
= \frac{1}{2} \text{tr} \left( \alpha \alpha^T - K^{-1} \partial K \partial \theta_j \right) \text{ with } \alpha = K^{-1} y
\]  

GPs are however computationally expensive to learn especially in an online setting. Sparse Pseudo-input Gaussian Processes (SPGPs) aim at reducing the complexity of GPs in both learning and prediction. The idea is to parametrize the regression model with the so-called pseudo-inputs. The location of these inputs is iteratively fitted by maximizing a new kind of marginal likelihood. Interestingly, using only a small amount of pseudo-inputs, SPGPs are capable of attaining very similar fitting and prediction results to normal GPs. To clarify, the idea is to parametrize the model by \( M << n \) pseudo-input points, while still preserving the full Bayesian framework. This leads to the parametrization of the covariance function by the location of \( M << n \) pseudo-inputs. These are then fitted in addition to the hyperparameters in order to maximize the following new marginal likelihood:

\[
p(y|X, \Theta) = \int p(y|X, \tilde{X})p(\tilde{X}|X)\text{d}\tilde{X}
\]

\[
= \mathcal{N}(y|0, K_{NM}^{-1}K_{MN} + \Lambda + \sigma^2 I),
\]

where, \( \tilde{X} \) is the matrix formed by the pseudo-inputs with \( \tilde{X} = \{\tilde{x}_m\}_{m=1}^{M} \), \( K_{NM} \) is the covariance matrix formed by the pseudo and the real inputs as \( K_{MN} = k(x_m, x_n) \) with \( k(\cdot, \cdot) \) being the covariance kernel. \( K_{M}^{-1} \) is the inverse of the covariance matrix formed among the pseudo inputs with \( K_{M} = k(x_m, x_m) \). \( \Lambda \) is a diagonal matrix having the diagonal entries of \( \lambda_n = k_{n n} - k_{M}^T K_{M}^{-1} k_{n} \). The noise variance and the identity matrix are represented by \( \sigma \) and \( I \), respectively.

Results in [22] show a complexity reduction in the training cost (i.e., the cost of finding the parameters of the covariance matrix) to \( O(M^2 N) \) and in the prediction cost (i.e., prediction on a new set of inputs) to \( O(M^2) \). The results further demonstrate that SPGPs can fully match normal GPs with small \( M \) (i.e., few pseudo-inputs), successfully producing very sparse solutions. A full mathematical treatment may be found elsewhere [22].

2.3 Transfer Learning

Transfer Learning (TL) is a technique used to counter the tabula rasa approach used often in machine learning [16]. The idea of TL is to reuse knowledge obtained through previous learning tasks (namely source tasks) when dealing with a new learning task (namely target task). In its most basic form, there exists a source and a target task where learning in the source task was accomplished at some earlier time and the knowledge acquired (in whatever form) is available for use in the target task. The main assumption made in any TL scheme ([8, 17, 23]) is that the source and target task can be found similar in some sense.

TL can be used to bias learning in a new learning task with the intention to reduce the amount of experience needed to learn an equally successful model. This makes TL ideally suited to strengthen any learning done within a restricted scenario like those of automated negotiation, where the amount of experience to learn from is limited.

In this paper, we adapt two different transfer learning algorithms for automated negotiation tasks. The first algorithm based on the instance transfer learning approach. The instance transfer learning
approach is intuitively appealing: although the whole data from source task cannot be reused directly, there are certain parts of the data that can still be reused together with a few labelled data in the target task [17]. Precisely, the idea is to reuse source data in the target task to increase the amount of learning data available. One of the most widely used instance transfer learning algorithm is TreAdaBoost, which was proposed to transfer instances between a source and a target task for classification. In the automated negotiation scenario, encountered offers from previous negotiation session are transferred to improve the learning agent’s offer proposition scheme in the ongoing negotiation session.

The second algorithm is based on the model transfer learning approach. Model transfer approach assumes that the source tasks and the target tasks are somehow related, and thus the models learnt from previous (source) tasks are still useful to a new (target) task. By means of discovering the relation between source and target models, knowledge can be transferred across tasks. Therefore, such kind of approach aims at retaining and applying the models learned in a single or multiple source tasks to efficiently develop an effective model for the target task, after seeing only a relatively small number of sample situations. In the automated negotiation scenario, instead of directly transfer the encountered offers from previous sessions, the learned models on historical negotiation sessions are transferred to approximate the model of the current session. It can automatically balance an ensemble of models with each trained on one known opponent.

3. TRANSFER BETWEEN NEGOTIATION TASKS

This section details the context and the proposed algorithms for automatically transferring between two or multiple negotiation tasks within the same domain. Next, a generic framework of negotiation strategy is first given, which support both transfer and non-transfer modes. The details of the learning in each of the source and the target tasks are then presented.

3.1 The Generic Framework of Agent-based Negotiation Strategy

In the present subsection, we detail the generic strategy framework. When the source task data is available, the strategy operates in the transfer learning mode to reuse knowledge from other negotiations tasks; in the other case, it works in the plain mode and decides its negotiation moves solely on the newly learnt model of the target task.

Upon receiving a counter-offer from the opponent at the time \( t_c \), the agent records the time stamp \( t_c \) and the utility \( U(\text{opp}) \) of this counter-offer according to its own utility function. A small change in utility of the opponent can result in a large utility variation for the agent leading to a fatal misinterpretation of the opponent’s behaviour in the case of multi-issue negotiations. Therefore and in order to reduce that negative impact, the whole negotiation is divided into a fixed number (denoted as \( \zeta \)) of equal intervals. The maximum utilities at each interval with the corresponding time stamps, significantly scales down the computation complexity of modelling opponent so that the response speed is improved.

Then, dependent on whether the source task data is available, the agent learns the opponent differently as explained in Section 3.2 and 3.3, respectively. With the approximated opponent model, the agent adopts a linear concession strategy to avoid further computation load. More specifically, the optimal expected utility \( \hat{u} \) (i.e., the expected maximum opponent concession) provided by the opponent model is used to set the target utility to offer at the current time \( t_c \) as follows:

\[
u^t = \hat{u} + (u_{\text{max}} - \hat{u})(\hat{q} - t_c)^\alpha
\]

where \( u_{\text{max}} \) is the maximum utility allowed in the negotiation task, \( \hat{q} \) is the time when \( \hat{u} \) will be reached, \( \alpha \) the concession factor determining the way how the agent concedes, (e.g., boulware \((\alpha < 1)\), conceder \((\alpha > 1)\) or linear \((\alpha = 1)\).

After the target utility \( u^t \) has been chosen, the agent has to decide how to respond to the opponent’s current counter-offer (this corresponds to line 14 in Algorithm 1). The agent first checks whether any of the following two conditions is fulfilled: 1) the utility of the latest counter-offer \( U(\text{opp}) \) is not smaller than \( u^t \); 2) the counter-offer has been proposed by the agent itself to its opponent at some earlier point during the ongoing negotiation process.

The agent settles the deal and the negotiation ends (line 12) if any of these two conditions is satisfied. Otherwise, the agent checks whether \( u^t \) falls below the best counter-offer received so far. If this holds, then, for the consideration of efficiency, this counter-offer is proposed to the opponent. Proposing such an offer is reasonable because it tends to satisfy the expectation of the opponent. If not, the agent then constructs a new offer following a \( \epsilon \)-greedy strategy as used in [4]. According to this strategy, a greedy offer is chosen with probability \( 1 - \epsilon \) in order to further explore the opponent behavior, and with probability \( \epsilon \) a random offer is made (where \( 0 \leq \epsilon \leq 1 \)). The greedy offer is chosen as follows. For a rational opponent, it is reasonable to assume that the sequence of its counter-offers is in line with its decreasing satisfaction. Thus, the more frequent and earlier a value of an issue \( j \) appears in counter-offers, the more likely it is that this issue contributes significantly to the opponent’s overall utility. Formally, let \( F(\cdot) \) be the frequency function defined by:

\[
F^n(v_{jk}) = F^{n-1}(v_{jk}) + (1 - t)^\psi \cdot g(v_{jk})
\]

where the superscript of \( F(\cdot) \) indicates the number of negotiation rounds, \( \psi \) is the parameter reflecting the time-discounting effect, and \( g(\cdot) \) is a two-valued function whose output is 1 if the specific issue value (i.e., \( v_{jk} \)) appears in the counter-offer and 0 otherwise.

The new offer to be proposed is the one whose issue values have the maximal sum of frequencies according to the frequency function and whose utility is not worse than the current target utility. In the case of a random offer, an offer whose utility is within a narrow range around \( u^t \) is randomly generated and proposed.

3.2 Learning in the Source Task

When no source tasks are at hand, the agent simply learns the current task using the plain mode of the proposed strategy. The source negotiation task starts by any side of the two parties presenting an offer describing values for the different negotiation issues. If an offer is accepted the negotiation session ends. On the other hand, if the offer is rejected the agent proposes a new offer to the other party. Then, the opponent can decide, according to her own behaviour model, whether to accept or reject this new offer.

While the opponent’s behaviour model is unknown, it can be learned over time. The opponent model is indirectly observed from the utilities of the opponent’s counter-offers: every time the opponent model is used to set the target utility to offer at the current time \( t_c \) as follows:

\[
u^t = \hat{u} + (u_{\text{max}} - \hat{u})(\hat{q} - t_c)^\alpha
\]

where \( u_{\text{max}} \) is the maximum utility allowed in the negotiation task, \( \hat{q} \) is the time when \( \hat{u} \) will be reached, \( \alpha \) the concession factor determining the way how the agent concedes, (e.g., boulware \((\alpha < 1)\), conceder \((\alpha > 1)\) or linear \((\alpha = 1)\).

After the target utility \( u^t \) has been chosen, the agent has to decide how to respond to the opponent’s current counter-offer (this corresponds to line 14 in Algorithm 1). The agent first checks whether any of the following two conditions is fulfilled: 1) the utility of the latest counter-offer \( U(\text{opp}) \) is not smaller than \( u^t \); 2) the counter-offer has been proposed by the agent itself to its opponent at some earlier point during the ongoing negotiation process.

The agent settles the deal and the negotiation ends (line 12) if any of these two conditions is satisfied. Otherwise, the agent checks whether \( u^t \) falls below the best counter-offer received so far. If this holds, then, for the consideration of efficiency, this counter-offer is proposed to the opponent. Proposing such an offer is reasonable because it tends to satisfy the expectation of the opponent. If not, the agent then constructs a new offer following a \( \epsilon \)-greedy strategy as used in [4]. According to this strategy, a greedy offer is chosen with probability \( 1 - \epsilon \) in order to further explore the opponent behavior, and with probability \( \epsilon \) a random offer is made (where \( 0 \leq \epsilon \leq 1 \)). The greedy offer is chosen as follows. For a rational opponent, it is reasonable to assume that the sequence of its counter-offers is in line with its decreasing satisfaction. Thus, the more frequent and earlier a value of an issue \( j \) appears in counter-offers, the more likely it is that this issue contributes significantly to the opponent’s overall utility. Formally, let \( F(\cdot) \) be the frequency function defined by:

\[
F^n(v_{jk}) = F^{n-1}(v_{jk}) + (1 - t)^\psi \cdot g(v_{jk})
\]

where the superscript of \( F(\cdot) \) indicates the number of negotiation rounds, \( \psi \) is the parameter reflecting the time-discounting effect, and \( g(\cdot) \) is a two-valued function whose output is 1 if the specific issue value (i.e., \( v_{jk} \)) appears in the counter-offer and 0 otherwise.

The new offer to be proposed is the one whose issue values have the maximal sum of frequencies according to the frequency function and whose utility is not worse than the current target utility. In the case of a random offer, an offer whose utility is within a narrow range around \( u^t \) is randomly generated and proposed.
The idea of knowledge transfer is to re-weight instances/models from the source task such that it helps the target task agent in learning the target opponent’s behaviour model \( \Theta \).

1: **Require:** different distribution (i.e., source task) labelled data sets \( T_D \) (if available), same distribution data set \( T_S \), the base learning algorithm \( \Xi \), the maximum number of iterations \( N \), maximum time allowed \( t_{\text{max}} \), and \( t^{(k)} \) is the current time index.

2: while \( t^{(k)} < t_{\text{max}} \) do

3: Collect time stamp and utility and add to \( T_S \)

4: Set \( n \times \text{size}(T_S) \)

5: if no source data available then

6: \( \Theta \leftarrow \text{SPGPs}(T_S) \)

7: else

8: \( \Theta \leftarrow \left\{ \begin{array}{ll}
\text{TrAdaBoost.Nego}(T_D, T_S, N) & \text{instance transfer} \\
\text{ExpBoost.Nego}(H, T_S, m, N) & \text{model transfer}
\end{array} \right. \)

9: end if

10: \( u' \leftarrow \text{setTargetU}(\Theta, n) \)

11: if Acceptable then

12: an agreement reached

13: else

14: proposes a new offer

15: end if

16: Increment time index

17: end while

18: Terminate the negotiation session

The idea of knowledge transfer is to re-weight instances/models from the source task such that it helps the target task agent in learning the target opponent’s behaviour model \( \Theta \).

**Algorithm 1** The generic framework of negotiation strategy is described. Depending on whether source data are available, it operates in two different modes, namely, the plain and transfer mode. The idea of knowledge transfer is to re-weight instances/models from the source task such that it helps the target task agent in learning the target opponent’s behaviour model \( \Theta \).

1: **Require:** different distribution (i.e., source task) labelled data sets \( T_D \) (if available), same distribution data set \( T_S \), the base learning algorithm \( \Xi \), the maximum number of iterations \( N \), maximum time allowed \( t_{\text{max}} \), and \( t^{(k)} \) is the current time index.

2: while \( t^{(k)} < t_{\text{max}} \) do

3: Collect time stamp and utility and add to \( T_S \)

4: Set \( n \times \text{size}(T_S) \)

5: if no source data available then

6: \( \Theta \leftarrow \text{SPGPs}(T_S) \)

7: else

8: \( \Theta \leftarrow \left\{ \begin{array}{ll}
\text{TrAdaBoost.Nego}(T_D, T_S, N) & \text{instance transfer} \\
\text{ExpBoost.Nego}(H, T_S, m, N) & \text{model transfer}
\end{array} \right. \)

9: end if

10: \( u' \leftarrow \text{setTargetU}(\Theta, n) \)

11: if Acceptable then

12: an agreement reached

13: else

14: proposes a new offer

15: end if

16: Increment time index

17: end while

18: Terminate the negotiation session

The idea of knowledge transfer is to re-weight instances/models from the source task such that it helps the target task agent in learning the target opponent’s behaviour model \( \Theta \).

**Algorithm 2** TrAdaBoost.Nego \((T_D, T_S, N)\)

1: **Require:** source task data sets \( T_D = \{T_{D_1}, \ldots, T_{D_k}\} \), the target task \( T_S \), the base learning algorithm \( \Xi \), and the maximum number of iterations \( N \).

2: \( T = T_{D_1} \cup \ldots \cup T_{D_k} \cup T_S \)

3: \( w = \{w_{T_{D_1}}, \ldots, w_{T_{D_k}}, w_{T_S}\} \)

4: Initialize: the weight vector \( w^{(1)}(x_i) = \frac{1}{|T|}, \) for \((x_i, c(x_i)) \in T \). (Alternatively, the initial weights could be set with the user’s knowledge.)

5: for \( t = 1 \) to \( N \) do

6: Set \( p^{(t)} = w^{(t)} / Z^{(t)} \) \((Z^{(t)} \) is a normalizing constant) \( Z^{(t)} \)

7: Learn a hypothesis \( h^{(t)} : X \rightarrow Y \) by calling \( \Xi \) with the distribution \( p^{(t)} \) over the combined data set \( T_{D_1} \cup T_S \).

8: Compute the adjusted weighted prediction error of \( h^{(t)} \) on each instance of \( T_S \) using:

\[
\epsilon_{\text{adj}}^{(t)} = \sum_{i=1}^{|T_S|} \frac{p^{(t)}(x_i) e^{-h^{(t)}(x_i)} - e^{h^{(t)}(x_i)}}{p^{(t)}(x_i)}
\]

9: Choose the best hypothesis \( \tilde{h}^{(t)} \) such that the weighted error is minimal.

10: Set \( \beta^{(t)} = \frac{1}{2} \ln(1 + \epsilon_{\text{adj}}^{(t)}) \) and \( \beta_j = \frac{1}{2} \ln(1 + \sqrt{2 \ln(|T_{D_j}|/N)}) \), where \( T_{D_j} \subseteq T_D \)

11: Store \( \tilde{h}^{(t)} \) and \( \beta^{(t)} \).

12: Update the weight vector according to:

\[
w^{(t+1)} = \left\{ \begin{array}{ll}
\frac{w^{(t)}(x_i)}{e^{-\beta \epsilon^{(t)}_{\text{adj}}(x_i)}} & \text{for } x_i \in T_{D_j} \\
\frac{w^{(t)}(x_i)}{e^{-\beta \epsilon^{(t)}_{\text{adj}}(x_i)}} & \text{for } x_i \in T_S
\end{array} \right.
\]

13: end for

14: Output: \( h^{(t)}(x) = \sum_{i=1}^{N} \beta^{(t)} \tilde{h}^{(t)}(x) \).

3.3 Knowledge Transfer and Target Task Learning

3.3.1 Instance-based Transfer Approach

TrAdaBoost [8] is originally designed for instance-based transfer learning, however it overlooks difference among source tasks. In order to make it well suited for the described negotiation setting, an extension of the standard TrAdaBoost algorithm is proposed to transfer instances between multiple negotiation tasks. This extended version is achieved by combining the principles of TrAdaBoost with the ideas of dealing with multi-task scenarios discussed in [25] and those of modifying a boosting-based classification approach for regression in [9], which together successfully results in the new regression algorithm TrAdaBoost.Nego. This new approach is specified in Algorithm 2.

TrAdaBoost.Nego requires two data sets as input. The first is \( T_D \) which represents the different distribution data set from one (or more) previous task(s) \( T_{D_k} \), where \( T_{D_k} \subseteq T_D \). Since the source and the target opponent’s attain their utilities from different distributions, then the different distribution data is that of the source data. Namely, \( T_{D_k} = \{ (x_i^{(k)}, u_i^{(k)}) \}_{i=1}^{T_{D_k}} \), where \( u_i^{(k)} \) is the predicted source task’s utility determined according to Equation 7.

The second data set required by the transfer algorithm is the same distribution data set \( T_S \). The same distribution data set is the one from the target task having time steps as inputs and received utilities as outputs. To define \( T_S \) we have one of the following two options. In the first, some instances of \( T_S \) are set manually. This is a valid option if the designer has some background knowledge about the negotiation task. In the other case, the instances of \( T_S \) are attained automatically from the initial negotiation steps in the target task, where the offer proposition step depends only on the source task’s knowledge. In the present case, the behaviour of the opponent is monitored similar to the learning in the source task and the utilities of the counter-offers are computed and added to \( T_S \).
adjusted error is still in the range $[0, 1]$. Although a number of loss from a loosely related source task can be alleviated. In addition, of negative transfer caused by the imposition to transfer knowledge $T$ of the target task. The best hypothesis is then chosen such that the impact can be minimized. In this way, the impact of negative transfer caused by the imposition to transfer knowledge from a loosely related source task can be alleviated. In addition, the proposed extension adopts the way used in [9] to express each error in relation to the largest error at every iteration such that each adjusted error is still in the range $[0, 1]$. Although a number of loss functions are optional, our implementation employs the linear loss function as shown in line 8 because it is reported to work consistently well (18).

Once the extended version of $Tr$AdaBoost algorithm fully fits the weights, the agent proposes an offer according to the predicted output of the target task function approximator in line 14 of Algorithm 2. After receiving a counter-offer, the utility of this offer is calculated and added to $T_S$ so to be used in the next run of $Tr$AdaBoost.Nego.

3.3.2 Model-based Transfer Approach

ExpBoost.Nego is one of widely used approaches for model-based transfer learning. Different from the instance-based transfer method, ExpBoost.Nego makes use of prior knowledge through a group of models $\Theta_1, \Theta_2, \ldots, \Theta_B$, trained on each source data sets separately. At every iteration, it trains a new hypothesis on the weighted instances of the target task, and then combines different models in order to improve performance even if the target opponent is mostly unknown. In contrast with the instance transfer approach, only the weights of target instances are re-calculated at each run of the algorithm, and the updating rule is according to the performance of the resulting combination of hypotheses. More precisely, target instances are given more importance when they are not correctly predicted. This is because they are believed to be more informative for the next iteration and help the learning algorithm to get better estimators. In the end, the approach returns the target opponent behaviour model represented by the weighted median combination of the hypotheses.

When applying the model transfer algorithm ExpBoost to the kind of automated negotiation introduced in this work, two issues stand out. The first one has been discussed in [18], that is, at each boosting iteration, ExpBoost must select between either the newly learned hypothesis on the weighted target instances or a single expert from one of the source tasks, which potentially imposes restrictions on its learning ability. The second issue relates to the one we have already discussed before – how to modify the algorithm for regression. To solve the first issue, we consider to relax the hypothesis selection constraint by allowing a linear combination of the learnt hypotheses from source tasks and the additional hypothesis trained for the target task, to minimize the error at each iteration using least squares regression. To solve the second issue, the ideas of AdaBoost.R2 [9] to deal with the way of computing the adjusted error are then incorporated into the modified version of ExpBoost. The modified algorithm is referred to as ExpBoost.Nego and present it in Algorithm 3.

### 4. EXPERIMENTAL RESULTS AND ANALYSIS

The performance evaluation was done with GENIUS (General Environment for Negotiation with Intelligent multi-purpose Usage Simulation [11]). Known as a famous simulation environment, GENIUS is also adapted by the international Automated Negotiating Agents Competition (ANAC) [1] as the official competition platform. In this simulation environment an agent can negotiate with other opposing agents representing different strategies in a specified negotiation domain, where the utility function is defined by the preference of each negotiating party. The performance of an agent can be evaluated via its utility/score achievements.

Six domains with the largest outcome space3 are chosen from the pool of test domains created for the ANAC competitions. For negotiations in large domains, finding an offer that is acceptable to both parties becomes more of a challenge than in a small domain in the sense it is much feasible in small domains to propose a large or even the whole proportion of the possible proposals during the negotiation. These domains are therefore more complicated and computational expensive to explore, placing a big demand on the efficiency of the proposed learning schemes. The main characteristics of these domains are over viewed in Table 1 (with a descending order of the size of outcome space).

Next, we first select those source tasks that are similar to the target task for the agent to operate the proposed methods. In so doing, the difference between the behavior models in the source and target tasks is made small such that transfer can be smoothly

---

3Outcome space of a domain refers to the number of possible agreements that could be agreed upon between participants.

---

### Algorithm 3 ExpBoost.Nego ($H$, $T_S$, $m$, $N$)

1. **Require**: the target task data sets $T_S$ with size $m$, the pool of learnt model of previous tasks $H = \{\Theta_1, \Theta_2, \ldots, \Theta_B\}$, the base learning algorithm $\Xi$, and the maximum number of iterations $N$.
2. **Initialize**: the weight vector $w^{(1)}$ with each item equally being $\frac{1}{m}$.
3. **for** $t = 1$ **to** $N$ **do**
   4. Learn a hypothesis $h^{(t)}_{B+1} : \mathcal{X} \rightarrow \mathcal{Y}$ by calling $\Xi$ with the distribution $w^{(t)}$.
   5. $H_t = H \cup h^{(t)}_{B+1}$
   6. Find the linear combination $h^{(t)}$ of the hypotheses from $H_t$, which minimizes squared error on instances of $T_S$.
   7. **Compute** the adjusted prediction error $e^{(t)}$ of $h^{(t)}$:
      
      $e^{(t)} = \frac{|h^{(t)}(x^{(i)}) - c(x^{(i)})|}{p^{(t)}}$, where $p^{(t)} = \max_{i=1}^{m} |h^{(t)}(x^{(i)}) - c(x^{(i)})|$

   8. **Calculate** $e^{(t)} = \sum_{i=1}^{m} w_i^{(1)} e^{(t)}$
   9. **If** $e^{(t)} \leq 0$ **or** $e^{(t)} > 0.5$, **then** stop.
   10. **Let** $\alpha^{(t)} = \frac{e^{(t)}}{1-e^{(t)}}$.
   11. **Update** the weight vector $w^{(t+1)} = w^{(t)} (1-e^{(t)}) / Z^{(t)}$, where $Z^{(t)}$ is a normalizing constant.
   12. **end for**

13. **Output**: the weighted median of $h^{(t)}(x)$ for $\lceil N/2 \rceil \leq t \leq N$, using the weight of $\text{ln}(1/\alpha^{(t)})$. 

---
WholeSaler

by the transfer effect since the improvement made by the transfer is
pants lagged far behind that of our agents. We suspect that is caused
interesting observation is that the mean performance of all partici-
formance than the agent using the plain strategy in the four do-
documented by PNAgent.

The results are shown in Figure 1. Both the instance-transfer
agent and model-transfer agents successfully achieved better perfor-
ance than the agent using the plain strategy in the four do-\nmains. Moreover, the instance-transfer agent seemed to have a
stronger negotiation power than the model-transfer agent. Another
interesting observation is that the mean performance of all partici-
pants lagged far behind that of our agents. We suspect that is caused
by the transfer effect since the improvement made by the transfer is

done. Then, we run tournaments composed of a range of the state-
of-the-art agents. Moreover, the order of our agents encountering
other opposing agents is random, in other words, there is no any
guarantee about the similarity between source and target tasks in
this setting. Such tournaments are able to provide a measure of
effectiveness of negotiation strategies from a realistic perspective.
Finally, the empirical game theory (EGT) analysis [14] is applied to
the tournaments results. Through this analysis, the strategy robust-
ness can be well examined, which enables us to have a clear view
whether the transfer learning schemes also improve the robustness
of the plain strategy, or not.

4.1 Similar Source and Target Negotiation Tasks

In this set of experiments, we evaluate the performance of the
proposed methods given the transferred tasks are closely related to
the target task. Toward this end, we manually choose those ANAC
agents as the opposing agents in source tasks, which behave in a
similar way with the opponent in the target task. To illustrate the
difference of the two proposed learning schemes, we implement
each algorithm described in Section 3.3 with a distinct agent, under
name of ITAgent (for instance transfer) and MTAgent (for model
transfer). The plain strategy (for the case of no transfer) is imple-
mplemented by PNAgent.

The results are shown in Figure 1. Both the instance-transfer
agent and model-transfer agents successfully achieved better perfor-
ance than the agent using the plain strategy in the four do-
mains. Moreover, the instance-transfer agent seemed to have a
stronger negotiation power than the model-transfer agent. Another
interesting observation is that the mean performance of all partici-
pants lagged far behind that of our agents. We suspect that is caused
by the transfer effect since the improvement made by the transfer is

4.2 Negotiation Tournaments

The first set of experiments, while successful, did not tell any-
thing about how the developed strategies perform when the simi-
larinity between source and target tasks is not significant. In order
to address this issue in a reasonable way, we carried out negotia-
tion tournaments to observe agents’ performance in a more real-
listic setting. In the tournament, each agent competes against all
other agents in a random order. For each of the domains, we run a
tournament consisting of the nine agents (e.g., the top three agents
from respective ANAC 2012 and 2011 plus ITAgent, MTAgent and
PNAgent) ten times to get results with high statistical confidence.
For convenience of comparing performance across domains, nor-
malization is adopted and done in the standard way, using the max-
imum and minimum raw score obtained by all agents in each do-
main.

According to the results given in Table 2, ITAgent and MTA-
gen, benefiting from the novel transfer learning schemes, took
the first and second place, respectively. Both of them achieved a
better score compared to the plain strategy (PNAgent), with each
obtaining an improvement of 5.5% and 4.5%. Although ITAgent
performed better than the other transferring agent, the difference
was small (less than 1%). The three best agents of ANAC 2012
followed the two transferring agents, thus finishing third to fifth. The worst performers were those from ANAC 2011, whose per-
formance was clearly below the two top agents, namely, 18% on
average.

4.3 Empirical Game Theoretic Analysis

Till now, the performance of strategies was studied only from the
traditional mean-scoring perspective. This, however, did not reveal
information about the robustness of these strategies, for example,
how would the results change if the players are free to switch their
strategies to another one which could bring in a better individual
payoff? To address robustness appropriately, the technique of em-
pirical game theoretic (EGT) analysis [14] is applied to the tour-
naments results. The aim of using EGT is to search for pure Nash
equilibria in which no agent has an incentive to deviate from its cur-
rent strategy, or best reply cycle where there exist a set of profiles
(e.g., the combination of strategies chosen by players) for which a
path of deviations exists that connect them, with no deviation lead-
ing to a profile outside of the set. For brevity, the profiles in both
Nash equilibria and best reply cycle are called stable states after-
wards. Moreover, we consider deviations as those in [6] (the best
single-agent deviation). In such a deviation one agent unilaterally
changes the strategy in order to statistically improve its own profit, knowing the configuration of opponent strategies. The abbreviation for each strategy is indicated by the bold letter in Table 2. A profile (node) in the resulting EGT graph is defined by the mixture of strategies used by the players in a tournament. The first row of each node lists the three strategies, and the second row shows how many players use each strategy. The initial state of a tournament consists of four states. OMACAgent is voted by a number of 52 players, finishing in the first place despite being the best strategy. MTAgent, which is used by a total number of 52 players, is second best. As a result, OMACAgent is the robust strategy selected for the first round.

The final ranking of strategy robustness is illustrated in Table 3. Surprisingly, the most stable strategy is AgentLG, even though it failed to reach the highest score achievement in the tournaments. This is because this strategy manages to demonstrate more comprehensive negotiation ability in the sense it is capable of winning more negotiations (even with a relatively smaller advantage). By contrast, ITAgent is merely in the fifth place despite being the best performer of the previous tournaments. MTAgent is more robust than the other transferring agent and the plain strategy, finishing in the second place.

The EGT analysis suggests that the proposed model-transfer learning method is robust, and seemingly has the potential of being applied in a wider range of scenarios than the instance-transfer learning method.

### 5. RELATED WORK

Opponent modeling is assumed to be of key importance to performing well in automated negotiations [21]. Learning in the negotiation setting is however hampered by the limited information that can be gained about an opponent during a single negotiation session. To enable learning in this setting, various simplifying assumptions are made. For example, Lin et al. [15] introduce a reasoning model based on a decision making and beliefs updating mechanism which allows the identification of the opponent profile from a set of publicly available profiles. Another work [2] investigates online prediction of future counter-offers by using differentials, thereby assuming that the opponent strategy is defined using a combination of time- and behavior-dependent tactics [10]. Hou [12] employs non-linear regression to learn the opponent’s decision function in a single-issue negotiation setting with the assumption that the opponent uses a tactic from the three tactic families introduced in...
[10]. [3] use a three-layer artificial neural network to predict future counter-offers in a specific domain, but the training process requires a large amount of previous encounters, which is time-consuming as well as computationally expensive.

Recent work has started to focus on learning opponent’s strategy in a more practical situation (i.e., without those simplifying assumptions). Some good examples are [4, 5, 24]. Williams et al. [24] apply Gaussian processes regression model to optimize an agent’s own concession rate by predicting the maximal concession that the opponent is expected to make in the future. This approach, known as IAMhaggler2011, made the third place in ANAC 2011 [1]. Another successful GPs-based approach is described in [4], where the authors model opponents by means of sparse pseudo-input Gaussian processes to alleviate the computational complexity of opponent modeling. Chen and Weiss [5] develop a negotiating agent, under name of OMAC, which aims at learning an opponent’s strategy by analyzing its behavior through discrete wavelet transformation and cubic smoothing spline. OMAC also adapts its concession behavior in response to uncertainties in the environment. OMAC performed better than the five best agents of ANAC 2011 and was awarded the third place in ANAC 2012. Although these methods are proven useful in certain scenarios, they all suffer from insufficient training data when facing an unknown opponent in a new encounter, which results in a more or less inefficient learning process.

6. CONCLUSIONS AND FUTURE WORK

This paper proposes the first robust and efficient transfer learning algorithms in negotiation tasks. The transfer technique makes use of adaptation of TradA Boost and ExpBoost — two well known supervised transfer algorithms — to aid learning against a new negotiating opponent. Two strategy variants were proposed. In the first the target task agent makes decisions based on weighting the instances of source and target tasks, while in the second, the agent decides its moves depending on a weighting of the source and the target models. Experimental results show the applicability of both approaches. More specifically, the results show that the proposed agents both outperform state-of-the-art negotiating agents in various negotiation domains with a considerable margin. They further demonstrate that the model transfer learning is not only a boost to the strategy performance, but also results in an improved strategy robustness.

There are several promising future directions of this work. First, the quantification of negative transfer is an essential next research step. Furthermore, a thorough analysis of the relationships between the agents’ preferences and strategies in order to get a better understanding of transferring behavior among negotiating opponents. This understanding is also of relevance with respect to maximizing transfer stability. Last but not least, the extension of the proposed framework and strategies toward concurrent negotiations is an important issue of practical relevance that needs to be explored. In such settings, an agent is negotiating against multiple opponents simultaneously. Transfer between these tasks can serve as a potential solution for optimizing the performance in each of the negotiation sessions.

7. REFERENCES


